

Stage 7 PROMPT sheet

S7/1 Equivalent fractions, decimals & percentages

- Percentage to decimal to fraction

$$27\% = 0.27 = \frac{27}{100}$$

$$7\% = 0.07 = \frac{7}{100}$$

$$70\% = 0.7 = \frac{70}{100} = \frac{7}{10}$$

- Decimal to percentage to fraction

$$0.3 = 30\% = \frac{3}{10}$$

$$0.03 = 3\% = \frac{3}{100}$$

$$0.39 = 39\% = \frac{39}{100}$$

- Fraction to decimal to percentage

$$\frac{4}{5} = \frac{80}{100} = 80\% = 0.8$$



Change to 100

$$\frac{3}{8} = 3 \div 8 = 0.375 = 37.5\%$$

S7/2 Increase/Decrease by a percentage

- To increase £12 by 5%

$$= 1.05 \times \text{£}12 \quad (100\% + 5\% = 105\%)$$

OR

$$= \text{£}12 + 5\% \text{ of } \text{£}12$$

- To decrease £50 by 15%

$$= 0.85 \times \text{£}50 \quad (100\% - 15\% = 85\%)$$

OR

$$= \text{£}50 - 15\% \text{ of } \text{£}50$$

S7/3 Divide a quantity into a given ratio

~ Put headings

~ Find how many shares in total

~ Amount \div no. shares = value of one share

e.g. Divide £240 between A and B in ratio of 3:5

A : B

3 : 5 = 8 shares

One share = £240 \div 8 = £30

A = 3 shares = 3 \times £30 = £90

B = 5 shares = 5 \times £30 = £150

S7/4 Use proportional reasoning

- Change an amount in proportion

e.g. If 6 books cost £22.50

Find the cost of 11. (*find cost of 1 first*)

- Change amounts to compare

e.g. A pack of 5 pens cost £6.10

A pack of 8 pens cost £9.20

Which is the best buy? (*find cost of 40 of each*)

S7/5 Calculate with fractions

- Add & subtract fractions

~ Make the denominators the same

$$\text{e.g. } \frac{1}{5} + \frac{7}{10}$$

$$= \frac{2}{10} + \frac{7}{10}$$

$$= \frac{9}{10}$$

$$\frac{4}{5} -$$

$$= \frac{12}{15} - \frac{10}{15}$$

$$= \frac{2}{15}$$

- Multiply fractions

~ Write 7 as $\frac{7}{1}$

~ Multiply numerators & denominators

$$\text{e.g. } 5 \times \frac{2}{3}$$

$$= \frac{5}{1} \times \frac{2}{3}$$

$$= \frac{10}{3} = 3\frac{1}{3}$$

$$\frac{4}{5} \times \frac{2}{3}$$

$$= \frac{8}{15}$$

- **Divide fractions**

~Write 7 as $\frac{7}{1}$

~Flip numerator & denominator after \div

~Multiply numerators & denominators

e.g. $5 \div \frac{2}{3}$	$\frac{4}{5} \div \frac{2}{3}$
$= \frac{5}{1} \times \frac{3}{2}$	$= \frac{4}{5} \times \frac{3}{2}$
$= \frac{15}{2} = 7\frac{1}{2}$	$= \frac{12}{10} = 1\frac{2}{10} = 1\frac{1}{5}$

- **Calculate fraction of quantity**

To find $\frac{4}{5}$ of a quantity $\div 5 \times 4$

e.g. $\frac{4}{5}$ of £20 = $20 \div 5 \times 4 = \text{£}16$

S7/6 Solve an equation by trial & improvement method

~ Find 2 consecutive numbers that the solution lies between

~ Then choose the half way number

~ Keep making improvements until the required accuracy achieved

e.g. To solve $x^3 - 3x = 6$ (correct to 1dp)

Try x =	$x^3 - 3x$	Comment
2	$2^3 - 2 \times 2 = 4$	Too small
3	$3^3 - 3 \times 3 = 28$	Too big
2.5	$2.5^3 - 3 \times 2.5 = 8.125$	Too big
2.3	$2.3^3 - 3 \times 2.3 = 5.267$	Too small
2.4	$2.4^3 - 3 \times 2.4 = 6.624$	Too big
2.35	$2.35^3 - 3 \times 2.35 = 5.928$	Too small

Solution is nearer 2.4 than 2.3

So $x = 2.4$ (correct to 1dp)

S7/7 Solve linear equations

~Multiply out brackets first

~If there are letters on both sides get rid of the smaller first

~Do the same to both sides

e.g.

To solve $5(x - 3) = 3x + 7$ (expand bracket)

$$5x - 15 = 3x + 7 \quad (-3x \text{ from both sides})$$

$$2x - 15 = +7 \quad (+15 \text{ to each side})$$

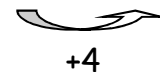
$$\frac{2x}{2} = \frac{22}{2} \quad (\div 2 \text{ both sides})$$

$$x = 11$$

S7/8 Sequences

- **Understand position and term**

Position	1	2	3	4
Term	3	7	11	15



+4

Term to term rule = **+4**

Position to term rule is $x \times 4 - 1$

(because position 1 $\times 4 - 1 = 3$)

nth term = $n \times 4 - 1 = 4n - 1$

- **Generate terms of a sequence**

If the nth term is $5n + 1$

1st term ($n=1$) = $5 \times 1 + 1 = 6$

2nd term ($n=2$) = $5 \times 2 + 1 = 11$

3rd term ($n=3$) = $5 \times 3 + 1 = 16$

S7/9 Plot graphs of linear equations

~Substitute values of x into the equation

~Plot the points in pencil

~Join the points with a ruler and pencil

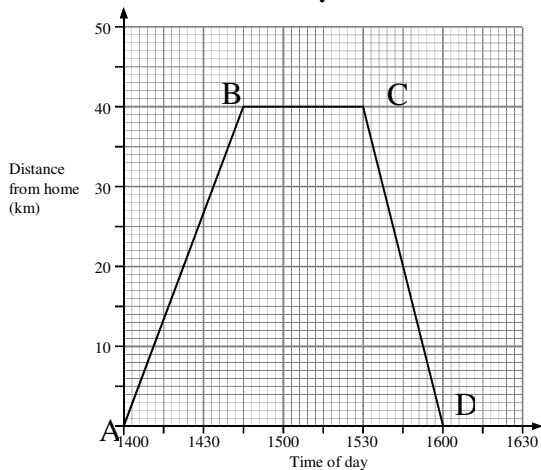
~They should be in a straight line

e.g. $y = 3x - 1$

x	-2	-1	0	1	2
y	-7	-4	-1	2	5

S7/10&11 Real life graphs

Some examples



- AB shows the journey away
- BC shows no movement
- CD shows journey back
- The steeper the line the higher the speed

Matching graphs to statements

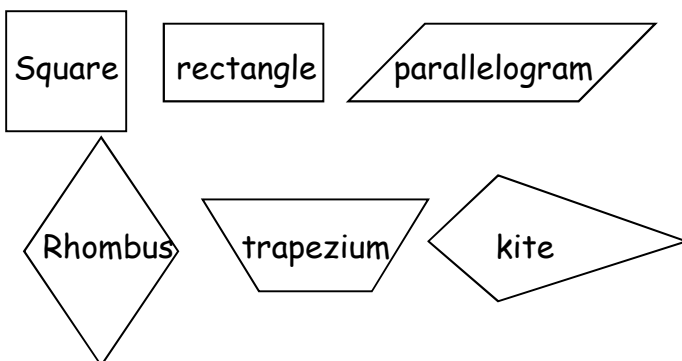


The price of oil, which was rising steadily at the beginning of the year, is now beginning to fall.	
Unemployment has been falling steadily over the last year.	
The birth rate was falling rapidly but is now steady.	
House prices, which were rising slowly, are now starting to rise rapidly.	

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S7/12 Quadrilaterals & their properties



- Know the name of each quadrilateral
- Does it have line and/or rotational symmetry?
- Are the diagonals equal or bisect each other?
- Does it have parallel sides?
- Are angles equal or opposites equal?

• Are the sides equal or opposites equal?

S7/13&14&15 Angles

• Angles & parallel lines

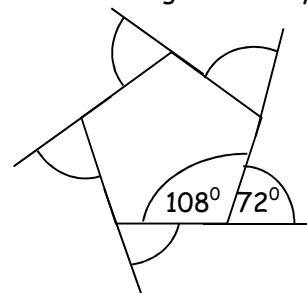
F-shape Corresponding angles are equal	Z-shape Alternate angles are equal	C or U shape Interior angles add up to 180°

• Angles and straight lines

Straight line = 180°	Opposite angles are equal

• Angles of polygons

- ~Polygons have straight sides
- ~Polygons are named by the number sides
 - 3 sides - triangle
 - 4 sides - quadrilateral
 - 5 sides - pentagon
 - 6 sides - hexagon
 - 7 sides - heptagon
 - 8 sides - octagon
 - 9 sides - nonagon
 - 10 sides - decagon
- ~With ALL sides equal they are called REGULAR
- ~ Sum of exterior angles is always 360°



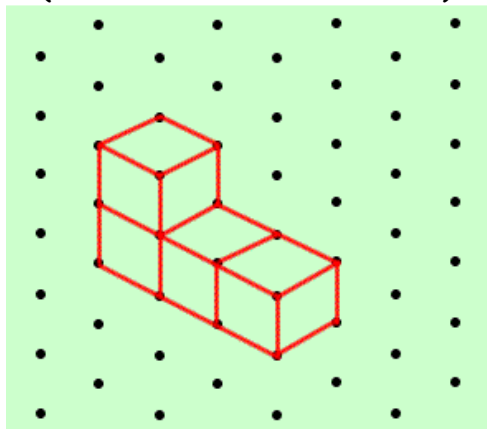
~ the interior & exterior angle add up to 180°

~ the interior angles add up to:

- Triangle = $1 \times 180^\circ = 180^\circ$
- Quadrilateral = $2 \times 180^\circ = 360^\circ$
- Pentagon = $3 \times 180^\circ = 540^\circ$
- Hexagon = $4 \times 180^\circ = 720^\circ$ etc

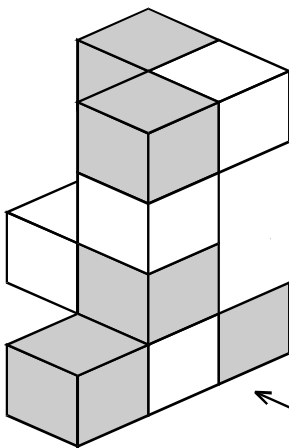
S7/16 2D representations of 3D shapes

- **3D drawing on isometric paper**
(notice NO horizontal lines)



- **3 views of a 3D shape**

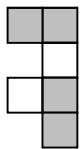
Plan view



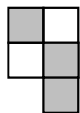
side-view

front elevation

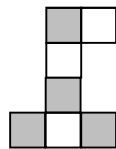
Side view



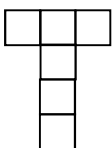
Plan view



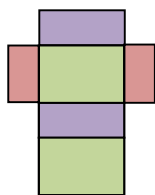
Front elevation



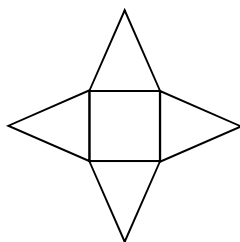
- **Nets**



Cube



Cuboid

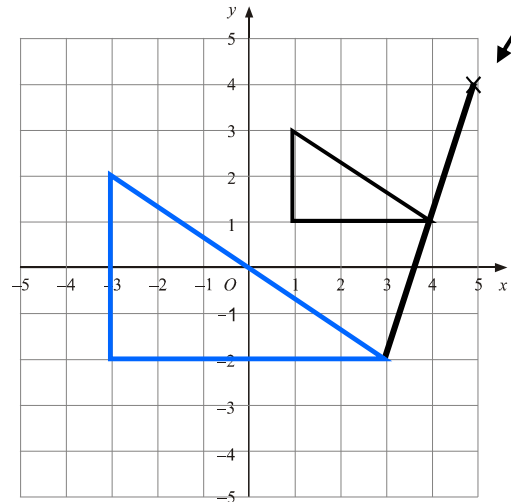


Square based pyramid

S7/17 Enlarge a shape

You need to know:

- Centre e.g. (5, 4)
- Scale factor e.g. 2

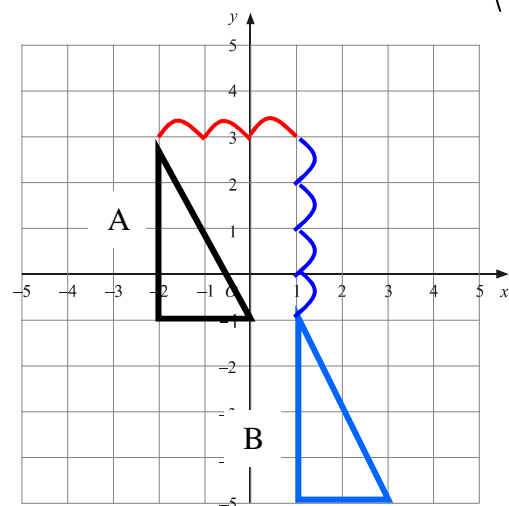


S7/18 Translate & Reflect a shape

- **Translate a shape**

You need to know:

- Vector from A to B e.g. $\begin{pmatrix} 3 \\ -4 \end{pmatrix}$ Right Down



Notice:

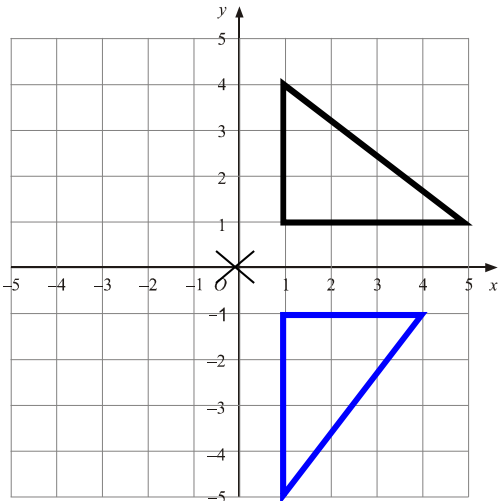
- The new shape stays the same way up
- The new shape is the same size

USE TRACING PAPER TO HELP

- **Reflect a shape**

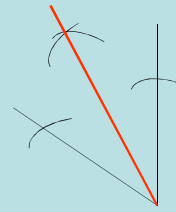
You need to know:

- Angle e.g. 90°
- Direction e.g. clockwise
- Centre of rotation e.g. $(0,0)$



USE TRACING PAPER TO HELP

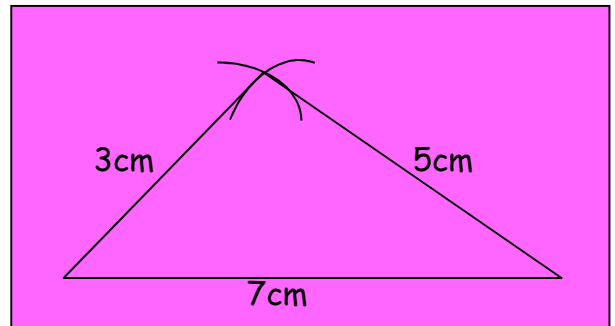
Draw a line from where the arcs cross to the vertex of the angle



- **Construct triangle given 3 sides**

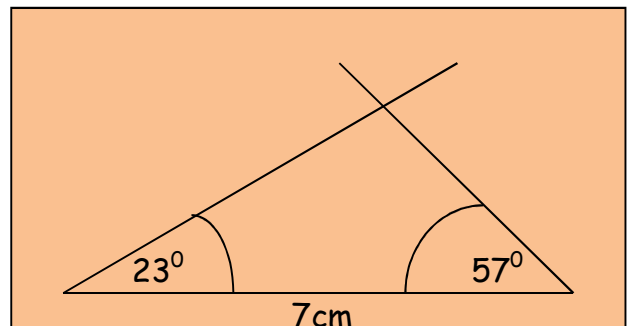
(Use a pair of compasses)

Leave the arcs on



- **Construct triangle given angles**

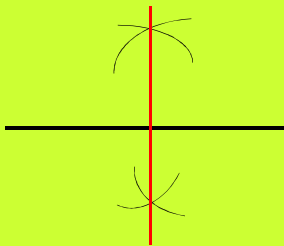
(Use a protractor)



S7/19 Constructions

- **Perpendicular bisector of a line**

Draw a straight line through where the arcs cross above and below.

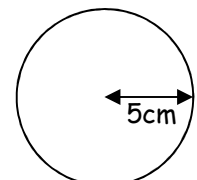


- **Bisector of a line**

S7/20 Use formulae

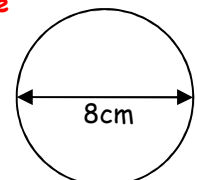
- **Area of circle**

$$\begin{aligned} \text{Area of circle} &= \pi \times r^2 \\ &= \pi \times 5^2 \\ &= \pi \times 25 \\ &= \underline{78.5\text{cm}^2} \end{aligned}$$



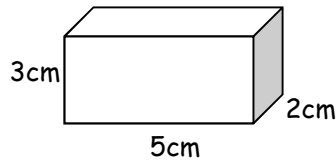
- **Circumference of circle**

$$\begin{aligned} \text{Area of circle} &= \pi \times d \\ &= \pi \times 8 \\ &= 25.1\text{cm} \end{aligned}$$



- **Volume of cuboid**

Volume = $l \times w \times h$
 $= 5 \times 3 \times 2$
 $= 30\text{cm}^3$



• **Surface area of cuboid**

Front = $5 \times 3 = 15$
 Back = $5 \times 3 = 15$
 Top = $5 \times 2 = 10$
 Bottom = $5 \times 2 = 10$
 Side = $3 \times 2 = 6$
 Side = $3 \times 2 = 6$

Total Surface Area = 62cm^2

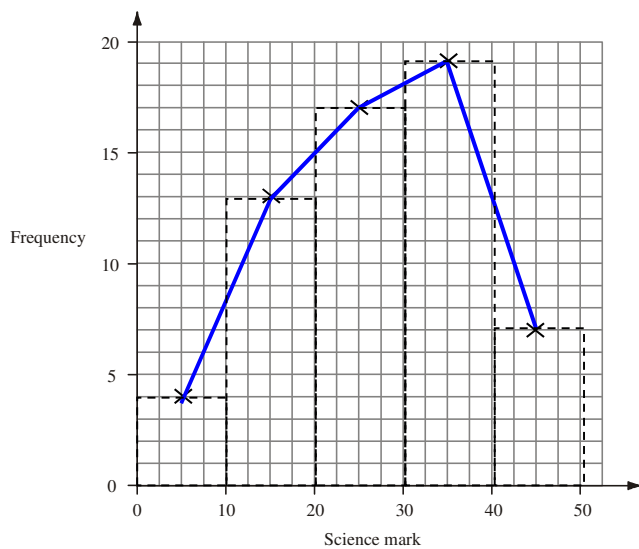
S7/23 Presentation of data

• **Construct a pie chart**

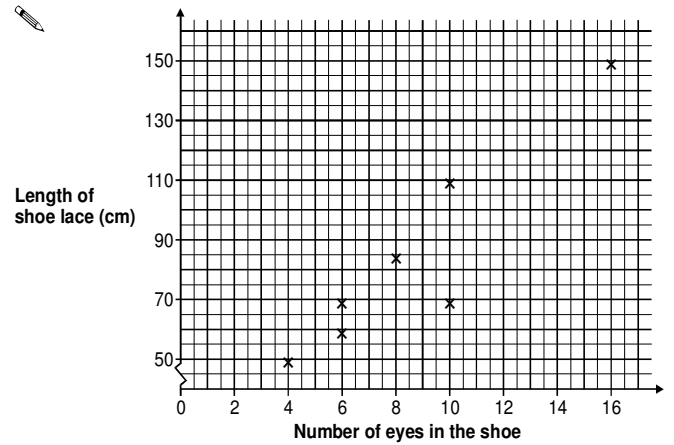
Transport	Frequency	Angle
Car	13×9	117°
Bus	4×9	36°
Walk	15×9	135
Cycle	8×9	72

Total frequency = 40
 $360^\circ \div 40 = 9^\circ$ per person

• **Construct a frequency polygon**
(points plotted at the midpoint of the bars)



• **Construct a scatter graph**



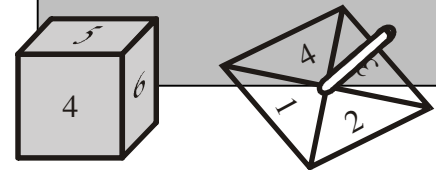
S7/24 Find all possible outcomes

Outcomes can be presented:

- In a list
- In a table or sample space

Example of a sample space

To show all possible outcomes from spinning a spinner and rolling a dice



		Dice						
		+	1	2	3	4	5	6
Spinner	1	2	3	4	5	6	7	
	2	3						
	3	4						
	4	5						

S7/25 Sum of mutually exclusive outcomes = 1

- If 2 outcomes cannot occur together, They are mutually exclusive
- If 2 outcomes A and B are mutually exclusive
 $P(A) + p(B) = 1$
- If 3 outcomes A B and C are mutually exclusive
 $P(A) + p(B) + p(C) = 1$

e.g. If outcomes A , B and C are mutually exclusive and

$$p(A) = 0.47$$

$$p(B) = 0.31$$

$$p(C) = 1 - (0.47 + 0.31)$$

$$= 1 - 0.78$$

$$= \underline{0.22}$$